

# An Integrated MCGDM Approach based Lean Facilitator Selection under Neutrosophic Environment

P Rajeswara Reddy, I Naga Raju, V Diwakar Reddy, G Krishnaiah

**Abstract**— In today's practical work environment group decision making is essential to choose best alternative from set of alternatives which are characterized by multiple criteria. In manufacturing environment frequent group decision making is common practice which involves conflicting and multiple criteria problems. In present Competitive world manufacturing advantage can be achieved by lean practices. The effective implementation of lean tools in any manufacturing industry requires efficient facilitator. Selection of lean facilitator is a complex multi criteria scenario. The proposed work paves a new integrated approach for user at ease of functioning and generating accurate results. The integrated approach combines AHP most popular method for deriving criteria weights and Technique for Order Preference by Similarity to Ideal Solution (TOPSIS) chosen as best recommended method to rank alternatives. The proposed work is carried out under Neutrosophic environment which can express incomplete, indeterminate and inconsistent information. Used predefine Interval Neutrosophic Values (INV) associates with linguistic attributes. The INV basic aggregating operators and score functions are applied in evaluating the AHP weights. Euclidean distances, and developed a MCGDM method based on similarity degree estimates rank of alternatives through TOPSIS. Concern topic reviews are also presented in this paper.

**Index Terms**— AHP, Interval Neutrosophic Values, MCGDM, Lean Facilitator, TOPSIS, Fuzzy Sets, Intuitionistic Fuzzy Sets

## 1 INTRODUCTION

Multi Criteria Decision Making (MCDM) is a strategy of evaluating practical complex situations based on various qualitative or quantitative criteria in certain or uncertain environments to recommend best choice among available alternatives. Several comparative studies [1a] have been taken to demonstrate its vast applicability [1b, 1c, 1d, 1e]. Briefing MCDM methods [1] will give clear understanding over techniques available [2] and benefits [1a]. More than one decision maker involve in decision making process stated as Multi Criteria Group Decision Making (MCGDM).

Analytical Hierarchy Process is most popular tool for complex decision making developed by Saaty [3a]. Compares relative priorities of criteria [4] gives weights of each criteria [3] and best supports complex MCDM problems. It is versatile tool [5] having wide flexibility of handle number of attributes in hierarchical manner [6].

In real world decision making conflicting, inconsistent, indeterminate information cannot be expressed in

terms of crisp values. Fuzzy Set (FS) theory [7] gives truth function which describes decision maker acceptance value to alternative categorized by an attribute. But the constraint lies, it doesn't represent false function. Atanassov introduce Intuitionistic Fuzzy Sets (IFS) [8,9] which can represent truth membership function  $T(x)$  as well as falsity membership function  $F(x)$ , they satisfy the condition  $T(x), F(x) \in [0,1]$  and  $0 \leq T(x)+F(x) \leq 1$ . In IFS the indeterminate function is rest of truth and false functions  $1-T(x)-F(x)$  that is indeterminate and inconsistency functions are not clearly defined. Samarandache [10] generalize FS, IFS, and Interval Valued Intuitionistic Fuzzy Set (IVIFS) [9] so on as Neutrosophic Set (NS) by adding indeterminate information. In NS the truth membership, indeterminacy membership, false membership functions are completely independent.

Recently, NS became interesting area for researcher to convert qualitative information into quantitative values which can express supporting, nondeterministic, rejection values in

terms of NS Values. Wang [12] propose Single Valued Neutrosophic Sets (SVNS) and Ye [13] gives correlation coefficient and weighted correlation coefficient in SVNS. Similar to IVIFS. Wang proposed Interval Neutrosophic Sets (INS) [14] in which the truth membership, indeterminacy membership, false membership functions were extended to interval values. Ye [15] given similarity measures between INSs based on Hamming and Euclidean distances demonstrate with a MCDM problem.

However, the proposed work is predefines INS values to represent linguistic attributes and derives the weight of criteria with aid of AHP and rank the alternatives by TOPSIS. In order to derive weights some of basic aggregation operations need to perform, given by [16]. As well as INS score and accuracy functions [17] are used to derive AHP weights. TOPSIS was developed by Hwang and Yoon [18]. It has extensive applicability of solving complex MCDM problems [19-26]. Based on INS Euclidean distances using similarity measuring [27] method rank the alternatives.

The rest of paper organized as follows. Section 2 basic definitions of Neutrosophic sets, briefing aggregation operators and score, distance measuring functions are given. In Section 3 methodology adopted is discussed. In Section 4 evaluation of case study with proposed method. In Section 5 conclusions are given.

## 2 Some Basic Theories on Neutrosophic Environment

### 2.1 INTERVAL NEUTROSOPHIC SETS (INS) [14]

The real scientific and engineering applications can be expressed as INS values.

Let  $X$  be a space of points (objects) and  $\text{Int} [0,1]$  be the set of all closed subsets of  $[0,1]$ . An INS  $\tilde{A}$  in  $X$  is defined with the form  $\tilde{A} = \{ \langle x, u_A(x), w_A(x), v_A(x) \rangle : x \in X \}$

Where  $u_A(x):X \rightarrow \text{int}[0,1]$ ,  $w_A(x):X \rightarrow \text{int}[0,1]$  and  $v_A(x):X \rightarrow \text{int}[0,1]$  with  $0 \leq \sup u_A(x) + \sup w_A(x) + \sup v_A(x) \leq 3$  for all  $x \in X$ . The intervals  $u_A(x)$ ,  $w_A(x)$  and  $v_A(x)$  denote the truth membership de-

gree, the indeterminacy membership degree and the falsity membership degree of  $x$  to  $\tilde{A}$ , respectively.

For convenience, if let  $u_A(x) = [u_A^-(x), u_A^+(x)]$ ,  $w_A(x) = [w_A^-(x), w_A^+(x)]$  and

$v_A(x) = [v_A^-(x), v_A^+(x)]$ , then  $\tilde{A} = \{ \langle x, [u_A^-(x), u_A^+(x)], [w_A^-(x), w_A^+(x)], [v_A^-(x), v_A^+(x)] \rangle : x \in X \}$

With the condition,  $0 \leq \sup u_A(x) + \sup w_A(x) + \sup v_A(x) \leq 3$  for all  $x \in X$ . Here, we only consider the sub-unitary interval of  $[0,1]$ .

Therefore, an INS is clearly neutrosophic set.

### 2.2 COMPLIMENT OF INS [15]

The complement of an INS  $\tilde{A}$  is denoted by  $\tilde{A}^c$  and is defined as  $u_A^c(x) = v(x)$ ,  $(w_A^-)^c(x) = 1 - w_A^+(x)$ ,  $(w_A^+)^c(x) = 1 - w_A^-(x)$  and  $v_A^c(x) = u(x)$  for all  $x \in X$ . That is,  $\tilde{A}^c = \{ \langle x, [v_A^-(x), v_A^+(x)], [1 - w_A^+(x), 1 - w_A^-(x)], [u_A^-(x), u_A^+(x)] \rangle : x \in X \}$ .

### 2.3 INS SUBSETS [15]

An interval neutrosophic set  $\tilde{A}$  is contained in the other INS  $\tilde{B}$ ,  $\tilde{A} \subseteq \tilde{B}$ , if  $u_A^-(x) \leq u_B^-(x)$ ,  $u_A^+(x) \leq u_B^+(x)$ ,  $w_A^-(x) \geq w_B^-(x)$ ,  $w_A^+(x) \geq w_B^+(x)$  and  $v_A^-(x) \geq v_B^-(x)$ ,  $v_A^+(x) \geq v_B^+(x)$  for all  $x \in X$ .

### 2.4 INS EQUALITY [15]

Two INSs  $\tilde{A}$  and  $\tilde{B}$  are equal, can be written as  $\tilde{A} = \tilde{B}$ , if  $\tilde{A} \subseteq \tilde{B}$  and  $\tilde{B} \subseteq \tilde{A}$ .

### 2.5 ARITHMETIC WEIGHTED AVERAGE OPERATOR FOR INS [16]

Let  $\tilde{A}_k$  ( $k=1, 2, \dots, n$ )  $\in$   $\text{INS}(X)$ . The interval neutrosophic weighted average operator is defined by  $F_\omega = (\tilde{A}_1, \tilde{A}_2, \dots, \tilde{A}_n)$   
 $= \sum_{k=1}^n w_k \tilde{A}_k = 1$   
 $=$

$$\left( \left[ 1 - \prod_{k=1}^n (1 - u_{\tilde{A}_k}^-(x))^{w_k}, 1 - \prod_{k=1}^n (1 - u_{\tilde{A}_k}^+(x))^{w_k} \right], \left[ \prod_{k=1}^n (w_{\tilde{A}_k}^-(x))^{w_k}, \prod_{k=1}^n (w_{\tilde{A}_k}^+(x))^{w_k} \right], \left[ \prod_{k=1}^n (v_{\tilde{A}_k}^-(x))^{w_k}, \prod_{k=1}^n (v_{\tilde{A}_k}^+(x))^{w_k} \right] \right)$$

(Equation: 1)

Where  $\omega_k$  is the weight of  $\tilde{A}_k$  ( $k=1, 2, \dots, n$ ),  $\omega_k \in [0,1]$  and  $\sum_{k=1}^n \omega_k = 1$ . Principally, assume  $\omega_k = 1/n$  ( $k=1, 2, \dots, n$ ), then  $F_\omega$  is called an arithmetic average operator for INSs.

### 2.6 GEOMETRIC WEIGHTED AVERAGE OPERATOR FOR INS [16]

Let  $\tilde{A}_k (k=1,2,\dots,n) \in \text{INS}(X)$ . The interval neutrosophic weighted geometric average operator is defined by  $G_\omega=(\tilde{A}_1, \tilde{A}_2, \dots, \tilde{A}_n) = \prod_{k=1}^n \tilde{A}_k^{\omega_k} =$

$$\left( \left[ \prod_{k=1}^n (u_{\tilde{A}_k}^-(x))^{\omega_k}, \prod_{k=1}^n (u_{\tilde{A}_k}^+(x))^{\omega_k} \right], \left[ 1 - \prod_{k=1}^n (1 - w_{\tilde{A}_k}^-(x))^{\omega_k}, 1 - \prod_{k=1}^n (1 - w_{\tilde{A}_k}^+(x))^{\omega_k} \right], \left[ 1 - \prod_{k=1}^n (1 - v_{\tilde{A}_k}^-(x))^{\omega_k}, \left( 1 - \prod_{k=1}^n (1 - v_{\tilde{A}_k}^+(x))^{\omega_k} \right) \right] \right)$$

(Equation: 2)

Where  $\omega_k$  is the weight of  $\tilde{A}_k (k=1,2,\dots,n)$ ,  $\omega_k \in [0,1]$  and  $\sum_{k=1}^n \omega_k = 1$ . Principally, assume  $\omega_k=1/n (k=1,2,\dots,n)$ , then  $G_\omega$  is called a geometric average for INSs.

The above aggregation operators remain INS values. The emphasis on above definitions 2.13 and 2.14 can be defined as the arithmetic weighted average operator gives group influence and geometric weighted average operator gives individual influence. So, the geometric weighted average (GWA) operator more sensitive comparatively. For this reason the current work is carried out with GWA.

**2.8 INS SCORE FUNCTION [17]**

Let  $\tilde{A} = ([a, b], [c, d], [e, f])$  be an interval valued neutrosophic number, a score function  $L$  of an interval valued neutrosophic value, based on the truth-membership degree, indeterminacy membership degree and falsity membership degree is defined by

$$L(\tilde{A}) = \frac{2+a+b-2c-2d-e-f}{4} \quad \text{(Equation: 3)}$$

where  $L(\tilde{A}) \in [-1,1]$ .

**2.9 INS ACCURACY FUNCTION [17]**

Let  $A = ([a, b], [c, d], [e, f])$  be an interval valued neutrosophic number. Then an accuracy function  $N$  of an interval neutrosophic value, based on the truth membership degree, indeterminacy membership degree and falsity membership degree is defined by

$$N(\tilde{A}) = 1/2(a+b-d(1-b)-c(1-a)-f(1-c)-e(1-d)) \quad \text{(Equation: 4)}$$

where  $L(\tilde{A}) \in [-1,1]$ .

**2.10 INS RANKING [27]**

Suppose that  $\tilde{A}_1 = ([a_1, b_1], [c_1, d_1], [e_1, f_1])$  and  $\tilde{A}_2 = ([a_2, b_2], [c_2, d_2], [e_2, f_2])$  are two interval valued neutrosophic sets. Then we define the ranking method as follows:

- (i) If  $L(\tilde{A}_1) > L(\tilde{A}_2)$ , then  $\tilde{A}_1 > \tilde{A}_2$ .
- (ii) If  $L(\tilde{A}_1) = L(\tilde{A}_2)$  and  $N(\tilde{A}_1) > N(\tilde{A}_2)$ , then  $\tilde{A}_1 > \tilde{A}_2$ .

**2.11 INS DISTANCE MEASURING FUNCTIONS [27]**

Let  $x = ([T_1^L, T_1^U], [I_1^L, I_1^U], [F_1^L, F_1^U])$ , and  $y = ([T_2^L, T_2^U], [I_2^L, I_2^U], [F_2^L, F_2^U])$  be two INVs, then

(1) The Hamming distance between  $x$  and  $y$  is defined as follows (Equation: 5)

$$d_H(x, y) = \frac{1}{6} \left( |T_1^L - T_2^L| + |T_1^U - T_2^U| + |I_1^L - I_2^L| + |I_1^U - I_2^U| + |F_1^L - F_2^L| + |F_1^U - F_2^U| \right)$$

(2) The Euclidian distance between  $x$  and  $y$  is defined as follows. (Equation: 6)

$$d_E(x, y) = \sqrt{\frac{1}{6} \left( (T_1^L - T_2^L)^2 + (T_1^U - T_2^U)^2 + (I_1^L - I_2^L)^2 + (I_1^U - I_2^U)^2 + (F_1^L - F_2^L)^2 + (F_1^U - F_2^U)^2 \right)}$$

**3. Methodology Adopted**

**Step 1:** Define a Multi Criteria Decision Making problem

**Step 2:** Obtain relative prioritized matrix of Criteria from each decision maker

**Step 3:** Use INS GWA (Equation: 2) operator to aggregate each decision matrix into a group decision matrix

**Step 4:** Derive weights of criteria aid of score function (Equation: 4) after row aggregation.

**Step 5:** Establish Criteria-Alternative group decision matrix using predefined attribute INS values

**Step 6:** Find Positive Ideal Solution (PIS) and Negative Ideal Solution (NIS) form step 5.

**Step 7:** Measure Euclidean distances (Equation: 6) of each alternative form PIS and NIS.

**Step 8:** Rank the alternatives based on Closeness Coefficient (CC) values. (Lower the CC value higher will be the rank)

**4. CASE STUDY**

**STEP 1:**

In dynamic global competition Lean implementation is key strategy for achieving organizational goals. The effective lean implementation can accomplish only by efficient Lean facilitator. Selection of Lean facilitator is a complex decision making problem characterized by

multiple criteria within several possibilities. The Lean facilitator is responsible for reducing or minimizing waste in overall plant and eliminating non value adding activities and maximizing total plant productivity resulting profits to the organization.

As stated above the Lean facilitator selection is multi criteria group decision making problem. It illustrates as follows.

**Group of Decision Makers (DM) are:**

{DM1, DM2, DM3}

DM1: Top Management, DM2: Professional Consultant, DM3: Operational Head

**Set of Criteria in order to select the alternatives are:**

{C1, C2, C3, C4, C5}

**C1. Educational Qualification:** The knowledge acquired through education is basic to understand fundamental concepts of Lean tools and techniques; this represents potential knowledge of the candidate. The relevant qualification will enhance candidate confidence in lean implementation.

**C2. Process Knowledge:** In order to apply the right Lean tool at the right place/ Process, the knowledge of process in the organization plays a vital role, so that Lean facilitator can apply right instrument of lean as per necessity.

**C3. Leadership Quality:** Lean facilitator should own the process of implementation and need to organize, control and guide teams of different levels of management and operators towards common goal. His leadership traits like communication, self-motivation showing the direction and giving right solution to the constraints at the right time plays vital role of success.

**C4. Experience/ Achievements:** The experience refers to the live scenarios faced in previous assignments/ projects and achievements reflects the level of accomplishment through received rewards and appreciation by management, peers etc., Which has significant weightage while choosing a right candidate for lean

facilitator at the organization in live scenario which gives higher operational achievements.

**C5. Report Writing:** An effective documentation skill in lean practices reduces the repeatability of tedious flow and information. Reporting of right information from the data will reduce the time and increases the effectiveness.

To maintain confidentiality the facilitators are named as {F1, F2, F3, F4, and F5}

**Table 1:** Predefined Linguistic Variables associated with Interval Valued Neutrosophic numbers

Very Low (VL)	[[0.1,0.2], [0.4,0.5], [0.5,0.6]]
Low (L)	[[0.3,0.4], [0.3,0.4], [0.2,0.3]]
Below Average(BA)	[[0.3,0.4], [0.2,0.3], [0.3,0.4]]
Average (A)	[[0.4,0.5], [0.2,0.3], [0.2,0.3]]
Above Average (AA)	[[0.4,0.5], [0.1,0.2], [0.2,0.3]]
Good (G)	[[0.5,0.6], [0.1,0.2], [0.1,0.2]]
Very Good (VG)	[[0.6,0.7], [0.1,0.2], [0.0,0.1]]
Excellent (E)	[[0.7,0.8], [0.0,0.1], [0.0,0.1]]

**Note:** The methodology simulated using MATLAB software

**STEP 2:**

**Table 2:** Relative prioritized criteria matrix of decision makers

Priorities	DM1	DM2	DM3
Education Knowledge	G	G	E
Leadership Quality	VG	E	G
Process Knowledge	E	E	AA
Experience/Achievements	VG	AA	G
Report Writing	E	G	VG

**STEP 3:**

**Table 3:** Aggregated Criteria matrix

Education Knowledge	[[0.5593 0.6604] [0.0678 0.1680 ] [0.0678 0.1680]]
Leadership Quality	[[0.5944 0.6952] [0.0678 0.1680] [0.0345 0.1347]]
Process Knowledge	[[0.5809 0.6840] [0.0345 0.1347] [0.0717 0.1723]]
Experience/Achievements	[[0.4932 0.5944] [0.1000 0.2000] [0.1037 0.2042]]
Report Writing	[[0.5944 0.6952] [0.0678 0.1680] [0.0345 0.1347]]

**STEP 4:**

**Table 4:** Score and Weights of each criterion

Criteria	Score	Weights
Education Knowledge	0.6701	0.1984
Leadership Quality	0.7042	0.2085
Process Knowledge	0.7043	0.2085
Experience/Achievements	0.5949	0.1761
Report Writing	0.7042	0.2085

**STEP 5:**

**Table 5:** Criteria-Alternative group decision matrix

Alternatives	Education Knowledge			Leadership Quality			Process Knowledge			Experience /Achievements			Report Writing		
	DM1	DM2	DM3	DM1	DM2	DM3	DM1	DM2	DM3	DM1	DM2	DM3	DM1	DM2	DM3
DM's															
Facilitator 1	VG	VG	G	G	VG	VG	VG	VG	G	G	VG	G	G	VG	G
Facilitator 2	G	AA	VG	G	AA	VG	A	AA	G	G	AA	G	G	AA	AA
Facilitator 3	G	VG	G	G	AA	G	VG	G	AA	G	G	VG	G	AA	G
Facilitator 4	G	G	G	AA	A	AA	VG	G	VG	G	AA	G	AA	A	AA
Facilitator 5	VG	G	G	G	G	AA	VG	VG	G	G	G	AA	E	G	VG

**STEP 6:**

For instance first column Positive and Negative Ideal solutions are given.

Positive Ideal Solution (PIS):

For all j  $\{[\max(a_{ij}) \max(b_{ij})] [\min(c_{ij}) \min(d_{ij})] [\min(e_{ij}) \min(f_{ij})]\}$

$\{[0.1316 \ 0.1693] [0.6766 \ 0.7610] [0.5649 \ 0.7116]\}$

Negative Ideal Solution (NIS): For all j  $\{[\min(a_{ij}) \min(b_{ij})] [\max(c_{ij}) \max(d_{ij})] [\max(e_{ij}) \max(f_{ij})]\}$

$\{[0.1089 \ 0.1420] [0.6766 \ 0.7610] [0.6808 \ 0.7637]\}$

**STEP 7:**

Euclidean distances: Derived from Equation 6  
(First column only)

Table 6: Euclidean Distance from PIS

F1	0
F2	0.0539
F3	0.0310
F4	0.0516
F5	0.0310

Table7: Euclidean Distance from NIS

F1	0.0539
F2	0
F3	0.0231
F4	0.0023
F5	0.0231

**STEP 8:** Ranking of alternatives is based on ratio of closeness coefficient  $Rcc_i = d_i^+ / (d_i^+ + d_i^-)$  (Equation: 7)

Rank order	Rcc <sub>i</sub>
F1	0.1016
F5	0.346
F3	0.5901
F4	0.7546
F2	0.8306

### 5. CONCLUSION

The selection of lean facilitator is conflict multi criteria group decision making problem. It is evaluated by newly proposed approach which hybridized AHP weighting method and TOPSIS ranking method, gives best result as comparatively. In order to reduce fuzzy and vagueness of subjective data given by decision makers the interval valued neutrosophic numbers are used. The proposed method gives the flexibility to decision maker's own choice for criterion weights instead of deviational weights. TOPSIS used to rank the facilitator under neutrosophic environment. Score function and Euclidean distances aided to evaluate ranks.

### REFERENCES

[1a] N Caterino, I Iervolino (2008), A Comparative Analysis Of Decision Making Methods For The Seismic Retrofit Of Rc Buildings, The 14<sup>th</sup>World Conference on Earthquake Engineering October 12-17, 2008, Beijing, China.  
 [1b] Milan Janic and Aura Reggiani (2002), An Application of the Multiple Criteria Decision Making (MCDM) Analysis to the Selection of a New Hub Airport, OTB Research institute Delft University of Technology Delft The Netherlands.

[1c] Aarushi Singh, Sanjay Kumar Malik (2014), Major MCDM Techniques and their application-A Review, M. Tech. Student, Hindu College of Engineering, Sonapat, IOSR Journal of Engineering (IOSRJEN) www.iosrjen.org ISSN (e): 2250-3021, ISSN (p): 2278-8719 Vol. 04.  
 [1d] Rohan K Gavade, Multi-Criteria Decision Making: An overview of different selection problems and methods, International Journal of Computer Science and Information Technologies, Vol. 5 (4) , 2014, 5643-5646.  
 [1] P.O. Box 64732, Virginia Beach, VA, 23467, An Analysis of Multi-Criteria Decision Making Methods, International Journal of Operations Research Vol. 10, No. 2, 56-66 (2013).  
 [2] E Triantaphyllou, Multi-Criteria Decision Making: An Operations Research Approach, *Encyclopedia of Electrical and Electronics Engineering*, (J.G. Webster, Ed.), John Wiley & Sons, New York, NY, Vol. 15, pp. 175-186, (1998).  
 [3] Thomas L Saaty, Decision making with the analytic hierarchy process, *Int. J. Services Sciences*, Vol. 1, No. 1, 2008.  
 [4] Evangelos Triantaphyllou, using the analytic hierarchy process for decision making in engineering applications: some challenges, *Inter'l Journal of Industrial Engineering: Applications and Practice*, Vol. 2, No. 1, pp. 35-44, 1995.  
 [5] Omkarprasad S. Vaidya, Analytic hierarchy process: An overview of applications, *European Journal of Operational Research* 169 (2006) 1-29.  
 [6] Adriyendi and Yeni Melia, DSS using AHP in Selection of Lecturer, *International Journal of Advanced Science and Technology* Vol. 52, March, 2013  
 [7] L A Zadeh, Fuzzy Sets, information and control 8, 338-353 (1965).  
 [8] K Atanassov (1994), Operators over interval-valued intuitionistic fuzzy sets, *Fuzzy Sets and Systems*, 64(2), 159-174.  
 [9] K Atanassov and G.Gargov, (1989).Interval-valued intuitionistic fuzzy sets, *Fuzzy Sets and Systems*, 31(3), 343-349.  
 [10] F Smarandache, (1999).A unifying field in logics. Neutrosophy: Neutrosophic probability, American Research Press, Rehoboth  
 [11] F.Smarandache (2005), A generalization of the intuitionistic fuzzy set. *International journal of Pure and Applied Mathematics*, 24, 287-297.  
 [12] H Wang, F Smarandache, and R.Sunderraman, (2010). Single valued neutrosophic sets, *Multispace and Multistructure* (4) 410-413.  
 [13] J Ye, (2013).Multicriteria decision-making method using the correlation coefficient under single-valued neutrosophic environment, *International Journal of General Systems* 42(4) 386-394.  
 [14] H Wang and F. Smarandache, Y. Q. Zhang, (2005). Interval neutrosophic sets and logic: Theory and applications in computing, Hexis, Phoenix, AZ.  
 [15] J Ye, (2014). Similarity measures between interval neutrosophic sets and their applications in Multi-criteria decision-making. *Journal of Intelligent and Fuzzy Systems* 26 165-172  
 [16] J Ye (2014). A multicriteria decision-making method using aggregation operators for simplified neutrosophic sets, *J. Intell. Fuzzy Syst.* 26 (5) 2459-2466.  
 [17] Ridvan Şahin, Multi-criteria neutrosophic decision making method based on score and accuracy functions under neutrosophic environment, Department of Mathematics, Faculty of Science, Ataturk University, Erzurum, 25240, Turkey  
 [18] C L Hwang and K. Yoon, Multiple Attribute Decision Making and Applications, Springer, New York, NY, 1981.  
 [19] T C Chen, Extensions of the TOPSIS for group decisionmaking under fuzzy environment, *Fuzzy Sets and Systems* 114(2000) 1-9.

[20] F Jin, P.D., Liu, X. Zhang, Evaluation Study of Human Resources Based on Intuitionistic Fuzzy Set and TOPSIS Method, *Journal of Information and Computational Science* 4(2007) 1023-1028.

[21] Y.Q.Wei, Risk Evaluation Method of Hightechnology Based on Uncertain Linguistic Variable and TOPSIS Method, *Journal of Computers* 4 (2009) 276-282.

[22] P.D.Liu, Multi-Attribute Decision-Making Method Research Based on Interval Vague Set and TOPSIS Method, *Technological and Economic Development of Economy* 15 (2009) 453-463.

[23] P.D. Liu & Y. Su, The extended TOPSIS based on trapezoid fuzzy linguistic variables, *Journal of Convergence Information Technology* 5 (2010) 38 - 53.

[24] P.D. Liu, An Extended TOPSIS Method for Multiple Attribute

Group Decision Making based on Generalized Interval-valued Trapezoidal Fuzzy Numbers, *Informatica* 35 ( 2011) 185-196.

[25] S. Mohammadi and N. Mousavi, Selecting adequate security mechanisms in e-business processes using fuzzy TOPSIS, *International Journal of Fuzzy System Application* 2(2012) 35-53.

[26] A.K. Verma & R. Verma, Facility location selection: an interval valued intuitionistic fuzzy TOPSIS approach, *Journal of Modern Mathematics and Statistics* 4 (2010) 68-72.

[27] Pingping Chi and Peide Liu (2013), An extended TOPSIS method for the multiple attribute decision making problems based on interval neutrosophic set, *Neutrosophic Sets and Systems, Vol.1*, China-Asean International College, Dhurakij Pundit University, Bangkok 10210, Thailand

IJSER